

A note on an area-type functional of Bloch functions

Kayumov I.

Kazan Federal University, 420008, Kremlevskaya 18, Kazan, Russia

Abstract

© 2017, Pleiades Publishing, Ltd. Let D be the unit disk centered at the origin in the complex plane. In this paper we consider an extremal problem for an area-type functional in the space B of Bloch functions with the seminorm $\|b\|_B = \sup\{(1 - |z|^2)|b'(z)| : z \in D\}$. We show that $\sup\{\sum_{k=1}^n k|b_k|^2 : \|b\|_B \leq 1\} = nB_n^2$, $n = 1, 2, 3, 4, 5$, where b_k are the Taylor coefficients of b and $B_n = \sup\{|b_n| : \|b\|_B \leq 1\}$.

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Keywords

area's functional, Bloch space

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